

203484 selected topic in  
transportation  
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# Introduction to MATLAB

# Outline

- Introduction and where to get MATLAB
- Data structure: matrices, vectors and operations
- Basic line plots
- File I/O

# Where to get MATLAB

- FAS computing:
  - Download from <http://fas.harvard.edu/computing/software/>
  - You must be on FAS network to use MATLAB
- HSEAS IT
  - Maxwell Dworkin Rooms G107-G111
- Mathworks:
  - Student version is affordable and complete.

# What is MATLAB

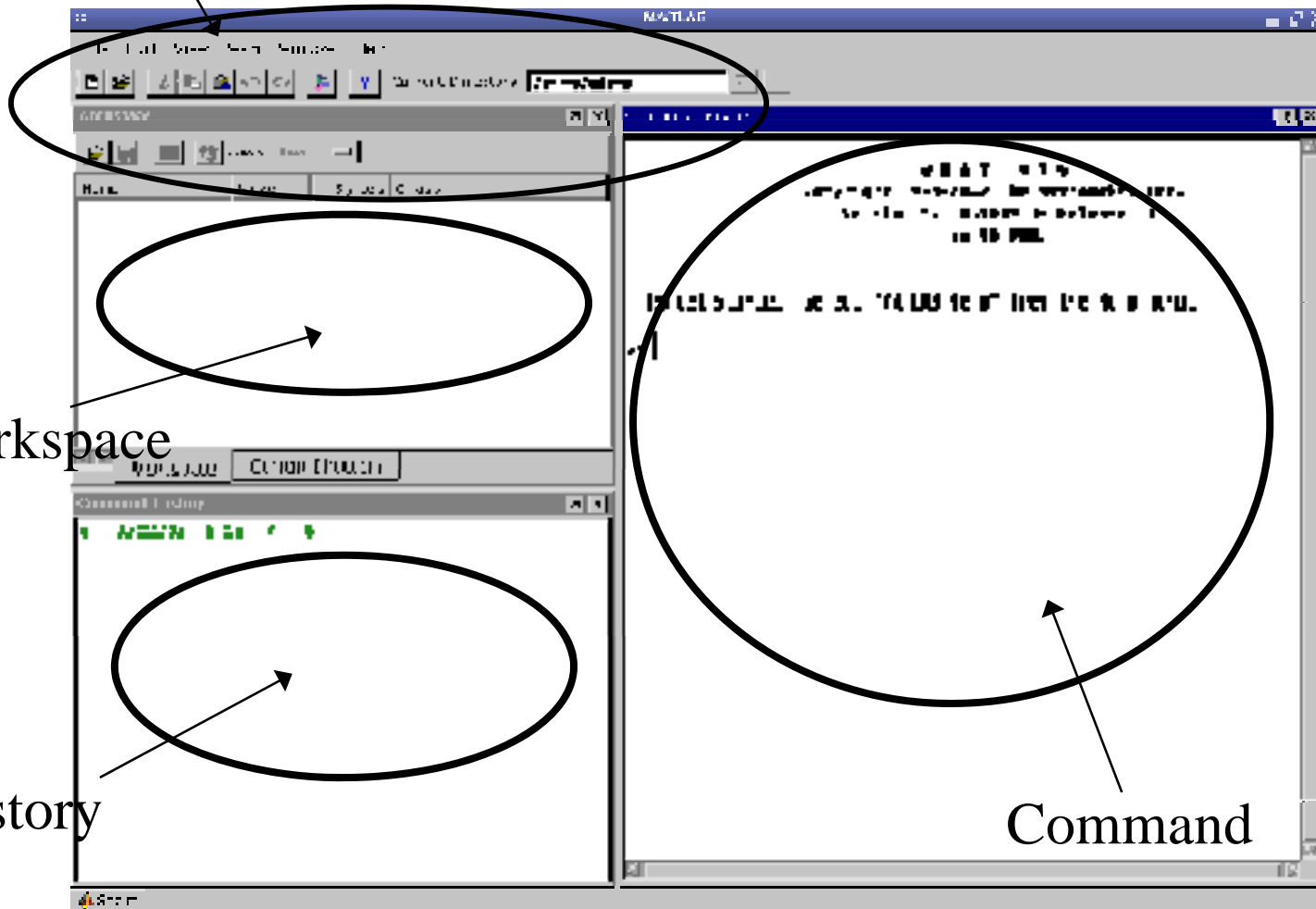
- High level language for technical computing
- Stands for **MA**TriX **LAB**oratory
- Everything is a matrix - easy to do linear algebra

# The MATLAB System

- Development Environment
- Mathematical Function Library
- MATLAB language
- Application Programming Language (not discussed today)

# MATLAB Desktop

Menu and toolbar



# Matrices & Vectors

- All (almost) entities in MATLAB are matrices

- Easy to define:

```
>> A = [16 3; 5 10]
A =
    16     3
     5    10
```

- Use ‘,’ or ‘ ’ to separate row elements -- use ‘;’ to separate rows

# Matrices & Vectors - II

- Order of Matrix -  $m \times n$ 
  - $m$ =no. of rows,  $n$ =no. of columns
- Vectors - special case
  - $n = 1$       column vector
  - $m = 1$       row vector



# Creating Vectors and Matrices

- Define

```
>> A = [16 3; 5 10]
A =
    16     3
     5    10

>> B = [3 4 5
        6 7 8]
B =
     3     4     5
     6     7     8
```

- Transpose

Vector :

```
>> a=[1 2 3];
```

```
>> a'
```

```
1
2
3
```

Matrix:

```
>> A=[1 2; 3 4];
```

```
>> A'
```

```
ans =
```

```
1     3
2     4
```

# Creating Vectors

Create vector with equally spaced intervals

```
>> x=0:0.5:pi
```

```
x =
```

```
0 0.5000 1.0000 1.5000 2.0000 2.5000 3.0000
```

Create vector with  $n$  equally spaced intervals

```
>> x=linspace(0, pi, 7)
```

```
x =
```

```
0 0.5236 1.0472 1.5708 2.0944 2.6180 3.1416
```

Equal spaced intervals in logarithm space

```
>> x=logspace(1, 2, 7)
```

```
x =
```

```
10.0000 14.6780 21.5443 ... 68.1292 100.0000
```

Note: MATLAB uses pi to represent  $\pi$ , uses i or j to represent imaginary unit

# Creating Matrices

- `zeros(m, n)` : matrix with all zeros
- `ones(m, n)` : matrix with all ones.
- `eye(m, n)` : the identity matrix
- `rand(m, n)` : uniformly distributed random
- `randn(m, n)` : normally distributed random
- `magic(m)` : square matrix whose elements have the same sum, along the row, column and diagonal.
- `pascal(m)` : Pascal matrix.

# Matrix operations

- $\wedge$  : exponentiation
- $*$  : multiplication
- $/$  : division
- $\backslash$  : left division. The operation  $A \backslash B$  is effectively the same as  $\text{INV}(A) * B$ , although left division is calculated differently and is much quicker.
- $+$  : addition
- $-$  : subtraction

# Array Operations

- Evaluated element by element
  - . ' : array transpose (non-conjugated transpose)
  - . ^ : array power
  - . \* : array multiplication
  - . / : array division
- Very different from Matrix operations

```
>> A=[1 2;3 4];  
>> B=[5 6;7 8];  
>> A*B  
    19    22  
    43    50
```

```
But:  
>> A.*B  
     5     12  
    21     32
```

# Some Built-in functions

- `mean(A)` : mean value of a vector
- `max(A)` , `min(A)` : maximum and minimum.
- `sum(A)` : summation.
- `sort(A)` : sorted vector
- `median(A)` : median value
- `std(A)` : standard deviation.
- `det(A)` : determinant of a square matrix
- `dot(a,b)` : dot product of two vectors
- `Cross(a,b)` : cross product of two vectors
- `Inv(A)` : Inverse of a matrix A

# Indexing Matrices

Given the matrix:

$A =$	$\longleftarrow$	$n$	$\longrightarrow$
	$\updownarrow$	$m$	
		0.9501	0.6068
		0.2311	0.4231
		0.4860	0.2774

Then:

$$A(1, 2) = 0.6068 \longrightarrow A_{ij}, i = 1 \dots m, j = 1 \dots n$$

$$A(3) = 0.6068 \longrightarrow \text{index} = (i - 1)m + j$$

$$A(:, 1) = \begin{bmatrix} 0.9501 \\ \uparrow \\ 1:m \\ 0.2311 \end{bmatrix}$$

$$A(1, 2:3) = [0.6068 \quad 0.4231]$$

# Adding Elements to a Vector or a Matrix

```
>> A=1:3
A=
     1     2     3
>> A(4:6)=5:2:9
A=
     1     2     3     5     7     9

>> B=1:2
B=
     1     2
>> B(5)=7;
B=
     1     2     0     0     7
```

```
>> C=[1 2; 3 4]
C=
     1     2
     3     4
>> C(3,:)=[5 6];
C=
     1     2
     3     4
     5     6

>> D=linspace(4,12,3);
>> E=[C D']
E=
     1     2     4
     3     4     8
     5     6    12
```



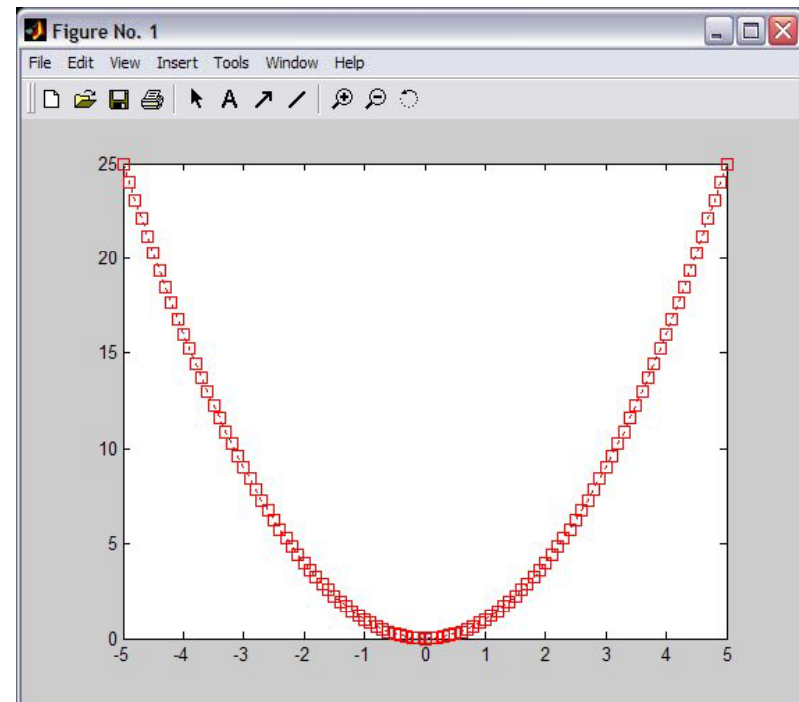
# Graphics - 2D Plots

```
plot(xdata, ydata, 'marker_style');
```

For example:

```
>> x=-5:0.1:5;  
>> sqr=x.^2;  
>> pl1=plot(x, sqr, 'r:s');
```

Gives:



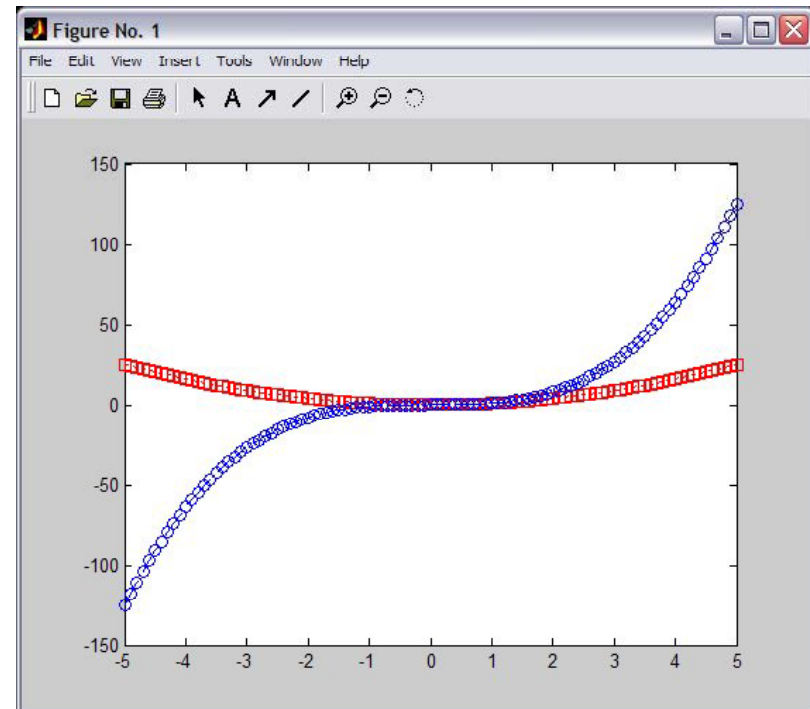
# Graphics - Overlay Plots

Use `hold on` for overlaying graphs

So the following:

```
>> hold on;  
>> cub=x.^3;  
>> pl2=plot(x, cub, 'b-o');
```

Gives:

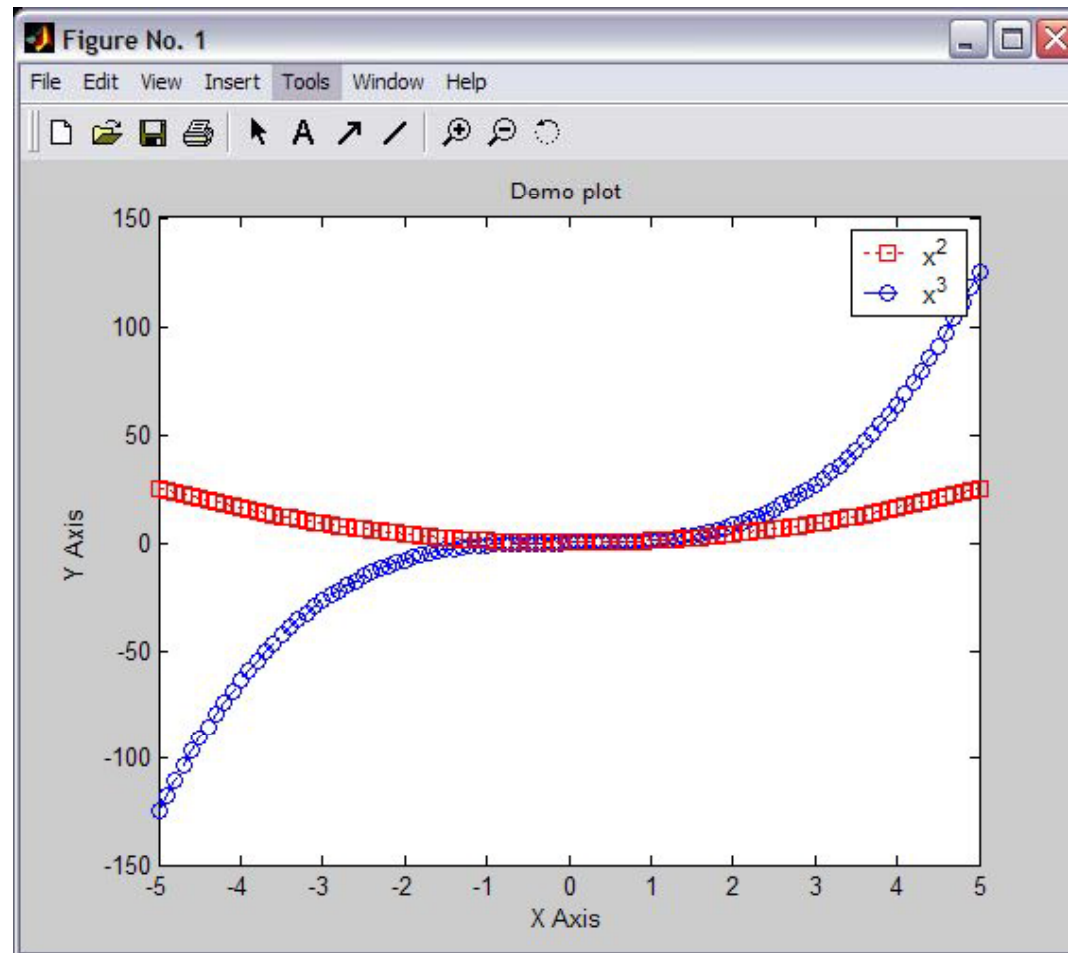


# Graphics - Annotation

Use `title`, `xlabel`, `ylabel` and `legend` for annotation

```
>> title('Demo plot');  
>> xlabel('X Axis');  
>> ylabel('Y Axis');  
>> legend([p11, p12], 'x^2', 'x^3');
```

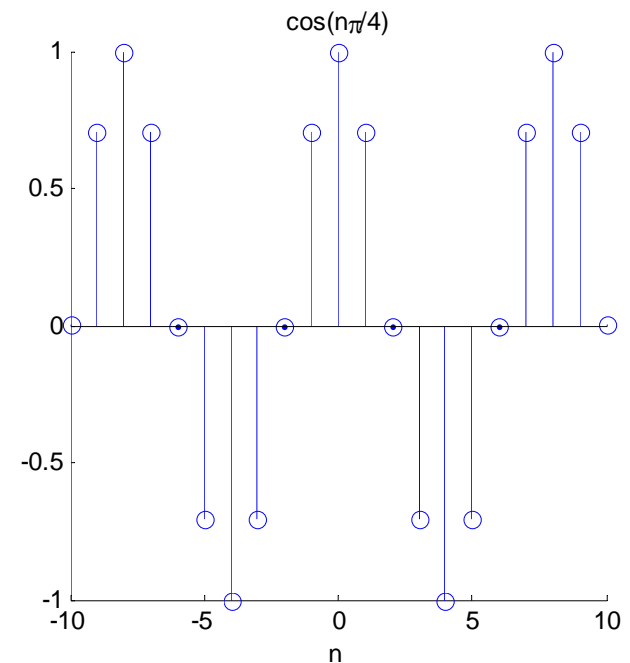
# Graphics - Annotation



# Graphics-Stem()

- `stem()` is to plot discrete sequence data
- The usage of `stem()` is very similar to `plot()`

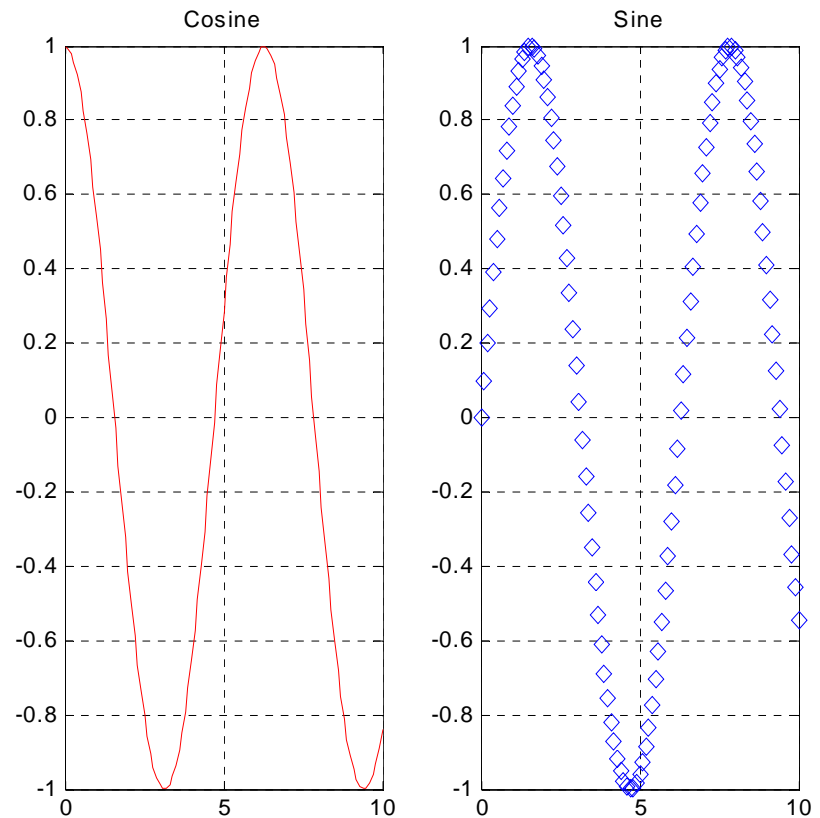
```
>> n=-10:10;  
>> f=stem(n,cos(n*pi/4))  
>> title('cos(n\pi/4)')  
>> xlabel('n')
```



# subplots

- Use subplots to divide a plotting window into several panes.

```
>> x=0:0.1:10;  
>> f=figure;  
>> f1=subplot(1,2,1);  
>> plot(x,cos(x),'r');  
>> grid on;  
>> title('Cosine')  
>> f2=subplot(1,2,2);  
>> plot(x,sin(x),'d');  
>> grid on;  
>> title('Sine');
```



# Save plots

- Use `saveas(h, 'filename.ext')` to save a figure to a file.

```
>> f=figure;  
>> x=-5:0.1:5;  
>> h=plot(x,cos(2*x+pi/3));  
>> title('Figure 1');  
>> xlabel('x');  
>> saveas(h,'figure1.fig')  
>> saveas(h,'figure1.eps')
```

Useful extension types:

bmp: Windows bitmap  
emf: Enhanced metafile  
eps: EPS Level 1  
fig: MATLAB figure  
jpg: JPEG image  
m: MATLAB M-file  
tif: TIFF image, compressed

# Workspace

- Matlab remembers old commands
- **And** variables as well
- Each Function maintains its own scope
- The keyword `clear` removes all variables from workspace
- The keyword `who` lists the variables



# File I/O

- Matlab has a native file format to save and load workspaces. Use keywords `load` and `save`.
- In addition MATLAB knows a large number of popular formats. Type `help fileformats` for a listing.
- In addition MATLAB supports ‘C’ style low level file I/O. Type `help fprintf` for more information.

# Practice Problems

- Plot the following signals in linear scale

$$x(t) = \sin(3t) \quad -5 < t < 5$$

$$y(t) = e^{2t+3} \quad 0 < t < 5$$

- Plot the following signals, use log scale for y-axis

$$x(t) = e^{t+2} (2t + 1) \quad 0 < t < 10$$

- Plot the real part and imaginary part of the following signal

$$x(t) = e^{0.5t + j(t + \pi/3)} \quad 0 < t < 10$$

- For the signal in previous question, plot its phase and magnitude