

แบบฝึกหัดปริพันธ์สองชั้น ชุดที่ 2

1. จงหาค่าของปริพันธ์ต่อไปนี้

1.1
$$\int_0^3 \int_{\sqrt{x/3}}^1 e^{y^3} dy dx$$

1.2
$$\int_0^2 \int_x^2 2y^2 \sin xy \, dy dx$$

1.3
$$\int_0^2 \int_0^{4-x^2} \frac{xe^{2y}}{4-y} dy dx$$

1.4
$$\int_0^1 \int_y^1 x^2 e^{xy} dx dy$$

1.5
$$\int_0^\pi \int_x^\pi \frac{\sin y}{y} dy dx$$

1.6
$$\int_0^8 \int_{\sqrt[3]{x}}^2 \frac{1}{y^4 + 1} dy dx$$

2. จงหาค่าของปริพันธ์ต่อไปนี้

2.1
$$\int_0^1 \int_0^{\sqrt{1-x^2}} (x^2 + y^2) dy dx$$

2.2
$$\int_0^2 \int_0^{\sqrt{2x-x^2}} \sqrt{x^2 + y^2} dy dx$$

2.3
$$\int_{-2}^2 \int_{-\sqrt{4-y^2}}^{\sqrt{4-y^2}} e^{-(x^2+y^2)} dx dy$$

2.4
$$\int_0^1 \int_0^{\sqrt{1-y^2}} \cos(x^2 + y^2) dx dy$$

2.5
$$\int_{-1}^1 \int_{\sqrt{1-y^2}}^{\sqrt{1-y^2}} (x^2 + y^2) dx dy$$

2.6
$$\int_0^1 \int_{-\sqrt{1-x^2}}^0 \frac{2}{1 + \sqrt{x^2 + y^2}} dy dx$$

2.7
$$\int_{-1}^1 \int_{-\sqrt{1-y^2}}^0 \frac{4\sqrt{x^2 + y^2}}{1 + x^2 + y^2} dx dy$$

2.8
$$\int_0^{\ln 2} \int_0^{\sqrt{(\ln 2)^2 - y^2}} e^{\sqrt{x^2 + y^2}} dx dy$$

2.9
$$\int_0^2 \int_0^{\sqrt{1-(x-1)^2}} \frac{x+y}{x^2 + y^2} dy dx$$

2.10
$$\int_0^2 \int_{-\sqrt{1-(y-1)^2}}^0 xy^2 dx dy$$

2.11
$$\int_{-1}^1 \int_{-\sqrt{1-y^2}}^{\sqrt{1-y^2}} \ln(x^2 + y^2 + 1) dx dy$$

2.12
$$\int_{-1}^1 \int_{-\sqrt{1-x^2}}^{\sqrt{1-x^2}} \frac{2}{(1 + x^2 + y^2)^2} dy dx$$

2.13
$$\int_0^1 \int_y^{\sqrt{y}} \sqrt{x^2 + y^2} dx dy$$

2.14
$$\int_{-2}^0 \int_{-\sqrt{4-x^2}}^0 \frac{1}{(1 + x^2 + y^2)^{3/2}} dy dx$$

2.15
$$\int_0^{\sqrt{2}} \int_y^{\sqrt{4-y^2}} \frac{1}{\sqrt{1 + x^2 + y^2}} dx dy$$

2.16
$$\int_{-3}^3 \int_0^{\sqrt{9-x^2}} \sin(x^2 + y^2) dy dx$$

2.17
$$\int_0^1 \int_y^{\sqrt{2-y^2}} (x+y) dx dy$$

2.18
$$\int_0^a \int_{-\sqrt{a^2-y^2}}^0 x^2 y dx dy \quad ; (a > 0)$$